

Predicate Calculus for Boolean Valued Functions. Part VIII

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Summary. In this paper, we proved some elementary predicate calculus formulae containing the quantifiers of Boolean valued functions with respect to partitions. Such a theory is an analogy of usual predicate logic.

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The articles [1], [6], [5], [8], [7], [4], [2], and [3] provide the notation and terminology for this paper.

In this paper Y is a non empty set.

One can prove the following proposition

- (1) For every element a of Boolean^Y and for every subset G of $\text{PARTITIONS}(Y)$ and for all partitions A, B of Y holds $\neg \exists \forall_{a,A} G, B G \in \exists \exists_{-a,B} G, A G$.

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