Predicate Calculus for Boolean Valued Functions.
Part IX

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Summary. In this paper, we proved some elementary predicate calculus formulae containing the quantifiers of Boolean valued functions with respect to partitions. Such a theory is an analogy of usual predicate logic.

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The articles [6], [9], [8], [7], [11], [10], [4], [5], [2], [1], and [3] provide the notation and terminology for this paper.

In this paper Y is a non empty set.

One can prove the following proposition

(3)[1] Let a be an element of $Boolean^Y$, G be a subset of PARTITIONS(Y), and A, B, C be partitions of Y. If G is independent, then $\neg \exists_{\forall_{a,A}G,B} G \Subset \neg \forall_{\forall_{a,B}G,A} G$.

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[1] The propositions (1) and (2) have been removed.

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